

2.3 Limits to infinity (end behavior)

2014-09-12 day 13

* The end behavior of a polynomial is determined by the end behavior of its ^{high} degree term.

[the high degree term dominates the end behavior]

* useful technique - factoring out powers of x [leaving negative powers of x]

* the "useful technique" (above) is also useful when radicals are involved, but requires more thought

* of course, for radicals, multiplying by a conjugate should also be considered.

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$$\lim_{x \rightarrow -\infty} \frac{4x^2 - x}{2x^3 - 5} = \lim_{x \rightarrow -\infty} \frac{x^2(4 - \frac{1}{x})}{x^2(2x - \frac{5}{x^2})}$$

$$\lim_{x \rightarrow -\infty} \frac{4 - \frac{1}{x}}{2x - \frac{5}{x^2}} = 0$$

strategy
form $\frac{\infty}{\infty}$
"cancel out infinities"

$$\lim_{x \rightarrow -\infty} x = -\infty$$

cp. to $\lim_{x \rightarrow -\infty} 2x = -\infty$

$$\lim_{x \rightarrow -\infty} cx = -\infty$$

$c > 0$ thank you
:-)

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$$\frac{4x^2 - x}{2x^3 - 5} = \frac{x^2 \left(4 - \frac{1}{x}\right)}{x^2 \left(2x - \frac{5}{x^2}\right)}$$

$$\begin{aligned} 4x^2 &= x^2 \square \\ \frac{1}{x^2} &= \frac{1}{x^2} \\ 4 &= \square \end{aligned}$$

$$\begin{aligned} x &= x^2 \square \\ \frac{1}{x^2} &= \frac{1}{x^2} \\ \frac{1}{x} &= \square \end{aligned}$$

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$$\lim_{x \rightarrow -\infty} \frac{4x^2 - x}{2x^3 - 5} = \lim_{x \rightarrow -\infty} \frac{x(4x - 1)}{x(2x^2 - \frac{5}{x})}$$

$$= \lim_{x \rightarrow -\infty} \frac{4x - 1}{2x^2 - \frac{5}{x}}$$

$$\lim_{x \rightarrow -\infty} \frac{4x^2 - x}{2x^3 - 5} = \lim_{x \rightarrow -\infty} \frac{x^3 \left(\frac{4}{x} - \frac{1}{x^2} \right)}{x^3 \left(2 - \frac{5}{x^3} \right)}$$

$$= \lim_{x \rightarrow -\infty} \frac{\frac{4}{x} - \frac{1}{x^2}}{2 - \frac{5}{x^3}} = \frac{0}{2 - 0} = 0$$

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$$\lim_{x \rightarrow -\infty} \frac{4x^2 - x}{2x^3 - 5} = \lim_{x \rightarrow -\infty} \frac{x^4 \left(\frac{4}{x^2} - \frac{1}{x^3} \right)}{x^4 \left(\frac{2}{x} - \frac{5}{x^4} \right)}$$

$$= \lim_{x \rightarrow -\infty} \frac{\frac{4}{x^2} - \frac{1}{x^3}}{\frac{2}{x} - \frac{5}{x^4}} = \frac{0-0}{0-0}$$

= $\frac{0}{0}$
indeterminate

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AP Calc Exam Tuesday 5/5

Section 1 { Part A: 28 questions, 55 minutes
multiple choice { no calculator
Part B: 17 q; 50 minutes
calculator

Section 2 { Part A: 2 q, 30 minutes
"free response" { calculator
FRQ
9 pts each { Part B: 4 q, 60 minutes
No calculator but.

$$\text{MC: } 45 \text{ q} \times 1.2 = 54$$

5 responses, but stupid ppl want to reduce this to 4

$$\text{FRQ: } 6 \text{ q} \times 9 \text{ pts} = 54$$

total: 108 pts

If there are clearly
n different
answers,
Each will
be graded
You will get
the average
rounding
down

essentially, in each q, the "readers"
look for 9 "good things" to say,
and you get a pt for each
you can say dumb stuff and lose
a "good thing" pt, But
you can't go negative.

On every test, there are "norm set"
questions that have been given before.
Your collective score on those n.s.g. determines
a "difficulty" rating for the test.

The cut scores will go up or down
depending on that difficulty

In other words, the ~~norm~~ scores are not curved
they are "managed"

my rule
of thumb: $75\% \approx 5$

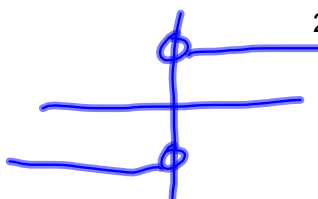
but the BC
exam also gives

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$$f(x) = \frac{x}{|x|}$$



$$\lim_{x \rightarrow +\infty} \frac{x}{|x|} =$$

$$\lim_{x \rightarrow \infty} \frac{x}{x} = 1$$

$$\lim_{x \rightarrow -\infty} \frac{x}{|x|}$$

$$\lim_{x \rightarrow -\infty} \frac{x}{(-x)}$$

$$= \lim_{x \rightarrow -\infty} -1 = -1$$

think
abs